

INTERVENTION TOOL

Lines and angles

1. Introduction

In order to develop a set of educational activities aimed to construct the meaning of relation between lines, transversals and angles, we refer to some theoretical frameworks that will be described in the session 2.

In session 3 the design of the educational activities is described. In particular, if the activities are addressed to students or the class, the educational aim of the activities, the Cognitive area and math domain of interest and the Mathematical objects in the areas of difficulties identified through the B2 questionnaire

2. Theoretical framework of reference

The theoretical references that helped us to design the following activities are:

1) Universal design for learning (UDL) principles (Table 3), a framework specifically conceived to design inclusive educational activities (http://udlguidelines.cast.org/)

Table 3: UDL guidelines



The Center for Applied Special Technology (CAST) has developed a comprehensive framework around the concept of Universal Design for Learning (UDL), with the aim of focusing research, development, and educational practice on understanding diversity and facilitating learning (Edyburn, 2005). UDL includes a set of Principles, articulated in



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*Guidelines and Checkpoints*¹. The research grounding UDL's framework is that "learners are highly variable in their response to instruction. [...]"

Thus, UDL focus on these individual differences as an important felement to understanding and designing effective instruction for learning.

To this aim, UDL advances three foundational Principles: 1) provide multiple means of representation, 2) provide multiple means of action and expression, 3) provide multiple means of engagement. In particular, guidelines within the first principle have to do with means of perception involved in receiving certain information, and of "comprehension" of the information received. Instead, the guidelines within the second principle take into account the elaboration of information/ideas and their expression. Finally, the guidelines within the third principle deal with the domain of "affect" and "motivation", also essential in any educational activity.

For our analyses we will focus in particular on specific guidelines within the three Principles². Guidelines within Principle 1 (provide multiple means of representation), suggest proposing different options for perception and offering support for decoding mathematical notation and symbols. Moreover, guidelines suggest the importance of providing options for comprehension highlighting patterns, critical features, big ideas, and relationships among mathematical notions. Finally, our analyses will give examples of how software AlNuSet can guide information processing, visualization, and manipulation, in order to maximize transfer and generalization.

Moreover, the guidelines from Principle 2 (provide multiple means of action and expression) suggest to offer different options for expression and communication supporting planning and strategy development. Finally, the guidelines from Principle 3 show how certain activities can recruit students' interest, optimizing individual choice and autonomy, and minimizing threats and distractions.

In the section 4 we will analyse examples of activities, classifying them both by the type of mathematical learning they are designed and the cognitive area they support. We will show how these examples have been designed on the UDL principles in order to make them inclusive and effective to overcome math difficulties identified through B2 questionnaire.

2) The European Project **FasMed**, that focused on formative assessment in mathematics and science, (<u>https://research.ncl.ac.uk/fasmed/</u>).

Formative assessment (FA) is conceived as a method of teaching where "evidence about student achievement is elicited, interpreted, and used by teachers, learners, or their peers, to make decisions about the next steps in instruction that are likely to be better, or better founded, than the decisions they would have taken in the absence of the evidence that was elicited" (Black & Wiliam, 2009, p. 7). FaSMEd project refers to Wiliam and Thompson (2007)'s study, that identifies five key strategies for FA practices in school setting: (a) *clarifying and sharing learning intentions and criteria for success;* (b) *engineering effective classroom discussions and other learning tasks that elicit evidence of student understanding;* (c) *providing feedback that moves learners forward;* (d) *activating students as instructional resources for one another;*-(e) *activating students as the owners of their own learning.* The teacher, student's peers and the student him- or herself are the agents that activate these FA strategies.

¹ For a complete list of the principles, guidelines and checkpoints and a more extensive description of CAST's activities, visit <u>http://www.udlcenter.org</u>

² The items are taken from the interactive list at <u>http://www.udlcenter.org/research/researchevidence</u>





Table 4: Formative assessment strategies

	Where the learner is going	Where the learner is right now	How to get there
Teacher	1 Clarifying learning intentions and criteria for success	2 Engineering effective class- room discussions and other learning tasks that elicit evidence of student understanding	3 Providing feedback that moves learners forward
Peer	Understanding and sharing learning intentions and criteria for success	4 Activating students as instructional resources for one another	
Learner	Understanding learning intentions and criteria for success	5 Activating students as the owners of their own learning	

FaSMEd activities are organized in sequences, that encompass group work on worksheets and class discussion where selected group works are discussed by the whole class, under the orchestration of the teacher. Taking into account formative assessment strategies and technology functionalities, Cusi, Morselli & Sabena (2017, p. 758) designed three types of worksheets for the classroom activity:

"(1) *problem worksheets:* worksheets introducing a problem and asking one or more questions involving the interpretation or the construction of the representation (verbal, symbolic, graphic, tabular) of the mathematical relation between two variables (e.g. interpreting a time-distance graph);

(2) *helping worksheets*, aimed at supporting students who face difficulties with *the problem worksheets* by making specific suggestions (e.g. guiding questions);

(3) poll worksheets: worksheets prompting a poll among proposed options".

The authors identified feedback strategies (Table 5) the teacher may adopt to give feedback to students (Cusi, Morselli & Sabena, 2018, p. 3466). These strategies are employed in the class discussion that is organized by the teacher after the group work on worksheets.

Table 5:

Revoicing	When the teacher mirrors one student's intervention so as to draw the attention on it. Often, during the revoicing, the teacher stresses with voice intonation some crucial words of the sentence she is mirroring. Rephrasing takes place when the teacher reformulates the intervention of one student, with the double aim of drawing the attention of the class and making the intervention more intelligible to everybody.	
Rephrasing	Rephrasing takes place when the teacher reformulates the intervention of one student, with the double aim of drawing the attention of the class and making the intervention more intelligible to everybody. Rephrasing is applied when the teacher feels that the intervention could be useful but needs to be communicated in a better way so as to become a resource for the others. [] The revoicing and rephrasing strategies [] turn one student (the author of the intervention) into a resource for the class.	
Rephrasing with scaffolding	When the teacher, besides rephrasing, adds some elements to guide the students' work.	



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Relaunching	When the teacher reacts to a student's intervention, which (s)he considers interesting for the class, not giving a direct feedback, but posing a connected question. In this way, by relaunching the teacher provides an implicit feedback [] on the student's intervention, suggesting that the issue is interesting and worth to be deepened or, conversely, has some problematic points and should be reworked on.
Contrasting	Contrasting takes place when the teacher draws the attention on two or more interventions, representing two different positions, so as to promote a comparison. By contrasting, [] the authors of the two positions may be resource for the class as well as responsible of their own learning.

We draw from the FaSMEd experience the idea of creating classroom activities in the formative assessment perspective, which may promote inclusion.

3. Design

3.1 Difficulties identified through the B2 questionnaire

We detect difficulties in the following item of B2:



Which sentences are true?

- a. Angles 1 and 4 are equal
- b. Angles 2 and 3 have the sum 180°
- c. Angles 1 and 2 have the sum 180°
- d. Angle 3 is greater than angle 2

These difficulties are related to remembering of the geometrical relationship.

3.2 Cognitive area and math domain of interest

The area of difficulties identified through the B2 questionnaire is related to the domain of *Geometry*. In particular, the difficulties are related to memorizing the geometrical relationship and decoding it correctly. Thus, *Memory* is the cognitive area involved (Table 1).





	Arithmetic	Geometry	Algebra
Memory		Which sentences are true? e. Angles 1 and 4 are equal f. Angles 2 and 3 have the sum 180° g. Angles 1 and 2 have the sum 180° h. Angle 3 is greater than angle 2	
Reasoning			
Visuo- spatial			

Table 1: The difficulties detected are linked to the cognitive domain of Memory and in the domain of Geometry

3.3 Educational Aims

The intervention tool is aimed at construct relations among Lines, Transversal and Angles.

3.4 Addressing to Student /class

The Intervention tool is articulated in a set of activities, taken from Desmos free application (https://www.desmos.com/?lang=it), that have to be carried out with all the class through on line teaching, in a perspective of inclusion.

3.5 Educational activities: the Intervention Tool

The teaching sequences are conceived to address specific learning difficulty, within an inclusive perspective. We suggest to follow with the all class the sequence of activities named "Lines, Transversals, and Angles" (https://teacher.desmos.com).

In this activity, students explore the relationship among angles formed by a transversal and a system of two lines. In particular, they consider what happens when the two lines are parallel vs. when they are not.

(See below a screenshot of the preview proposal).

















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In addition, as suggested in Desmos activities too, the teacher can promote a discussion to compare different solutions, to converge on a common definition, to support students with difficulties...

Discussion through UDL guidelines about the above-mentioned activities

We observe that the same educational aim of remembering the relations between angles in Geometry is approached in different ways by acting on the three principles of UDL (Table 7, in red our comments to illustrate the connection between the principles and our activities).

Engagement	Representation	Action & Expression
Recruiting interest	Perception	Physical Action
Optimize individual choice and autonomy	Offer ways of customizing the display of information	Vary the methods for response and navigation
Optimize relevance, value, and authenticity	Offer alternatives for visual information	
Minimize threats and distractions	Different registers through which information are displayed (visual; symbolic)	
Sustaining effort Persistence	Language & Symbols	Expression Communication
Heighten salience of goals and objectives	symbols	Use multiple tools for construction and composition
Vary demands and resources to optimize challenge	Offer alternative language and symbols to decode information and to work on	Build fluencies with graduated levels of support for practice and performance
Foster collaboration and community	the information Support decoding of text,	To use different registers in order to communicate
Increase mastery-oriented feedback	mathematical notation, and symbols This is promoted by the	This is promoted by the use of terms that are alternative to the formal ones to speak
Oriented feedbacks support engagement and motivation with respect the elaboration of the solution of the task	dynamic action, and by the manipulation of objects Promote understanding across languages	about mathematical objects. Moreover, in the activities virtual or concrete mathematical manipulatives are provided. For instance, dragging a moving point may help visualizing that the variable may have different values on the number line.

Table 7: Analysis of the activities through the Table of UDL principles.





Self Regulation	Comprehension	Executive functions
Promote expectations and beliefs that optimize	Activate or supply background knowledge	Guide appropriate goal- setting
motivation	Highlight patterns, critical	The use of artefacts may also
Facilitate personal coping skills and strategies	features, big ideas, and relationships (checkpoint 3.2)	Artefacts guide students' process of inquiry, providing
Develop self-assessment	Guide information processing	Support planning and strategy
	Maximize transfer and	development
Formative assessment	generalization	Facilitate managing
section 2, may help self-	Perception, language and	Enhance canacity for
More specifically, the teacher	(Constructing useable	monitoring progress
may provide different types of feedback	knowledge, knowledge that is accessible for future decision-	
	making, depends not upon	
	but upon active "information processing skills")	

This allows students to remember geometric relations at stake.

5. References

[1]Desmos : <u>https://www.desmos.com/?lang=it</u> [2]Karagiannakis, G. N., Baccaglini-Frank, A. E., & Roussos, P. (2016). Detecting strengths and weaknesses in learning mathematics through a model classifying mathematical skills. Australian J. of Learning Difficulties, 21(2), 115–141. [3]UDL Principles: <u>http://udlguidelines.cast.org/</u>

